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The Achromatic Interfero Coronagraph

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Abstract

We report on the Achromatic Interfero Coronagraph, a focal imaging device which aims at rejecting the energy contribution of a point-like source set on-axis, so as to make detectable its angularly-close environment (applicable to stellar environment: circumstellar matter, faint companions, planetary systems, but also conceivably to Active Galactic Nuclei and multiple asteroids).

With AIC, starlight rejection is based on destructive interference, which allows exploration of the star's neighbouring at angular resolution better than the diffraction limit of the hosting telescope. Thanks to the focus crossing property of light, rejection is achromatic thus yielding a large spectral bandwidth of work. Descriptions and comments are given regarding the principle, the device itself, the constraints and limitations, and the theoretical performance. Results are presented which demonstrate the close-sensing capability and which show images of a companion obtained in laboratory and “on the sky” as well. A short pictorial description of alternative AIC concepts, CIAXE and Open-Air CIAXE, currently under study, is given. *To cite this article: Y. Rabbia et al., C. R. Physique 8 (2007).*

Résumé

Le Coronographe Interférentiel Achromatique On présente le Coronographe Interférentiel Achromatique (AIC dans le texte), un système imageur en mode coronographique pour rejeter de l'image, la contribution d'une source ponctuelle sur l'axe de visée afin de laisser apparaître son environnement angulairement proche (cela concerne les étoiles : matière circumstellaire, compagnons faibles, systèmes exoplanétaires, mais potentiellement aussi les Galaxies à noyau actif et les astéroïdes multiples).

Avec le AIC, la réjection sur l'axe procède par interférences destructives, ce qui permet une exploration du voisinage stellaire dans une proximité angulaire meilleure que celle fixée par la limite de diffraction du télescope. Le principe de la réjection utilise le passage d'une onde par un foyer ce qui la rend achromatique et permet ainsi d'observer à large bande spectrale. On décrit le principe et l'architecture du coronographe, les contraintes instrumentales, les limitations associées, et les performances théoriques en réjection. Des résultats de tests, en laboratoire et en observation sur le ciel, sont donnés, en terme d'images montrant les capacités de sondage proche et de détection d'un compagnon faible. Une brève présentation graphique de deux concepts CIAXE et Open-Air CIAXE (actuellement en phase d'étude) dérivés du principe générique est donnée. *Pour citer cet article : Y. Rabbia et al., C. R. Physique 8 (2007).*

Key words: Stellar coronagraphy; High Contrast Imaging; Nulling Techniques

Mot-clés : Coronographie Stellaire; Imagerie à Haut Contraste; Interférométrie Annulante

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1. Introduction

The Achromatic Interfero Coronagraph (AIC in the following) is a focal imaging device working in coronagraphic mode and meant as a tool for the study of stellar environment (Gay & Rabbia [1]; Gay et al. [2]; Baudoz et al. [3,4]). The purpose of stellar coronagraphy is to make detectable images of the faint emitting features located angularly very close to an unresolved source whose brightness is tremendously larger (typically 10^4 to 10^6 times larger) than any of the surrounding features. This is the case for stars but also for other celestial sources as for example Active Galactic Nuclei and asteroids with multiple components. In the following we use “star” and “companion” to respectively denote the central source and any neighbouring feature. Any coronagraph aims at lowering as far as possible the energy contribution of the parent star in the recorded image, which would otherwise prevent the detection of the companion. The goal is thus to perform the “extinction” of the star while keeping the off-axis components transmitted as completely as possible to the detector in image plane. This extinction capability, is usually expressed by the “Rejection rate” defined by $Rej = F_{collected}/F_{residual}$, where $F_{residual}$ and $F_{collected}$ are the fluxes recorded with and without coronagraphic effect, respectively.

Not only the rejection capability is required but also the “close-sensing” capability : rejection must apply only within a very small angular extension, called the “Inner Working Angle” (IWA in the following) around the pointing direction, otherwise companions are also rejected.

In addition, the rejection ought to apply over as large as possible a spectral bandwidth, benefiting to the detection capabilities in several respects : increase of Signal to Noise Ratio (SNR), adaptability to science target by flexible choice of dedicated spectral intervals, enhancement of detectivity by a differential data processing, the “adapted scale image subtraction” (Gay et al. [5]; Rabbia et al. [6]) inspired by a method introduced by Racine et al. [7].

Early stellar coronagraphs have been a transposition to stars of the scheme initially introduced by B. Lyot (Lyot [8]) to study the solar corona. The technique relies on a tiny opaque mask set at the focus of an intermediate image plane, so as to block photons from the on-axis source, while photons from the companion are transmitted to the ultimate image plane. Because of diffraction effects the mask must cover several Airy radii (λ/D : working wavelength/diameter of the telescope) what makes the “close-sensing capability” comparatively poor (Mouillet et al. [9]; Beuzit et al. [10]).

Another approach, called interfero-coronagraphy, yields the extinction from a destructive interference process. The collected incident wave is splitted into two components, which are recombined after insertion of a π phase shift between them. Thus the recombination (coherent addition of fields at the detector) results in destructive interference and ideally no photon from the on-axis source can reach the detector. Here, thanks to the coherence properties of light, an angular sensing capability at a level better than the diffraction limit (λ/D), is achievable. The subsequent counterpart is a limitation of extinction (finite star size and random tilt of incident wavefront).

As early as 1996, the concept of the AIC has been suggested (Gay & Rabbia [1]; Gay et al. [2]) from which various prototypes have been developed and used for tests in laboratory (Baudoz [3]; Rivet et al. [11]) and “on the sky” (Baudoz et al. [4,12]) on ground-based telescopes (although AIC has been initially devised for space-based operation (Rabbia et al. [13])). Besides, even although coronagraphs are generally meant as working with single compact aperture, AIC can be used for nulling interferometry (Gay & Rabbia [1]; Rabbia et al. [14]), for example, in a two-aperture Bracewell configuration (Bracewell [15]). The immediate and essential requirement to obtain the coronagraphic effect with AIC is that the (complex) transmission of the aperture must be centro-symmetric (insensitive to a 180 degrees rotation).

Other concepts for interfero-coronagraphy, each using a specific type of beam separation/recombination have been devised since. Let us cite among other early concepts : the Phase Mask Coronagraph -PMC- (Roddier & Roddier [16]), the Sectorized Phase Mask Coronagraph -SPMC- (Rouan et al. [17]), and the Phase Knife Coronagraph -PKC- (Abe et al. [18]).

The main specific feature and advantage of AIC is the achromaticity of the phase shift process, which was not the case for the others cited, early interfero-coronagraph designs, and for the Lyot configuration as well. Another one regards the IWA, with the best close-sensing capability (Guyon et al. [19]). Another specific feature is that AIC yields two twin-images of the companion (displayed symmetrically with respect to the pointing axis), each conveying 1/4 of the collected energy. This can be seen as a drawback because of a reduced transmission and because of the symmetrization of companions (point-like or extended). Actually this is an advantage for point-like companions whose separations and orbits are better determined from the twin-images.

In this article we give but a kind of status report on the AIC (a comparison between AIC and other coronagraphs is given in Guyon et al. [19]) focusing, for the reader’s convenience, on the underlying algebraic formalism, though

recalling only basic lines because of space limitation. In Section 2 we describe the principle of the device and the device itself and we give a short pictorial description of alternative AIC devices, currently under study (Gay et al. [20,21]). In Section 3 we describe the constraints for both implementation and operation, and we outline the theoretically expected capabilities of AIC. In section 4 we give results from testing AIC both in laboratory and “on the sky”.

2. Basic principle

2.1. Functional description and pictorial summary

Basically, AIC is a Michelson-Fourier interferometer modified by inserting on one arm an achromatic π phase shift and a pupil rotation by 180 degrees. This double operation is performed by a cat’s eye optical system, where the π phase shift originates in the focus crossing property (Gouy [22]; Born & Wolf [23]; Boyd [24]). The collimated beam from the telescope is splitted in two sub-beams forming the two interferometric arms, one (the “fc” arm), where the focus-crossing occurs, the other (the “ff” arm) which includes a train of flat mirrors to balance the optical paths in the interferometer. In the design these optical paths are equal but some spurious residual Optical Path Difference (OPD) might still occur at the implementation and must be controlled. The beamsplitter at entry is used also for the recombination of beams. As a pictorial summary, Fig. 1 illustrates these comments. Mono-axial configurations, easier to insert in a telescope’s optical train, (Gay et al. [20,21]) have been devised,

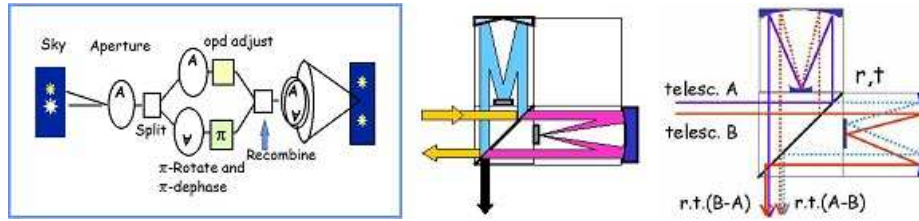


Figure 1. Schematic illustration of AIC functions (left) the configuration of beams in single aperture mode (center))the routing of beams with a two-aperture interferometer (right).

and are currently under study : the CIAXE and the open-air CIAXE. Fig. 2 schematically illustrates the paths of beams for the two concepts, and shows how the generic functions (beamsplitting, focus-crossing, recombination, zero-OPD) are performed.

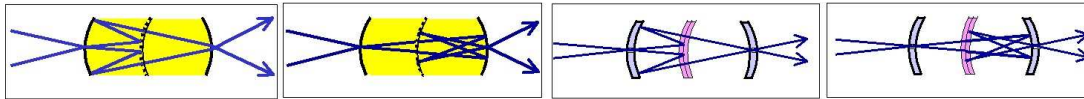


Figure 2. Schematic description with separated beam routes for CIAXE (left) and for Open-Air CIAXE (right), where generic functions of AIC appear. In CIAXE, beam entry and exit are small uncoated area, while they are holes in Open-Air CIAXE. Typical overall volume roughly is the one of a cylinder 4×3 mm length \times diameter.

2.2. Physical description

The typical AIC device consists of a kit of optical components assembled on a basement comprising two galleries for beams to travel in air. All elements are in Silica and assembling is made using molecular bonding under interferometric control. Optical paths are equalized by construction, however a fine-tuning of OPD (few nanometers) remains possible. The K photometric window, ($\lambda = 2.2 \mu\text{m}$, $\Delta\lambda = 0.4 \mu\text{m}$) being a convenient spectral interval (regarding both science and constraints), the beamsplitter cube is optimized for $\lambda = 2.2 \mu\text{m}$ but can work with a bandwidth larger than the K-band. The remaining components being mirrors are achromatic by nature. An incident collimated on-axis beam yields two perpendicular output beams. One, the constructive port, conveys all

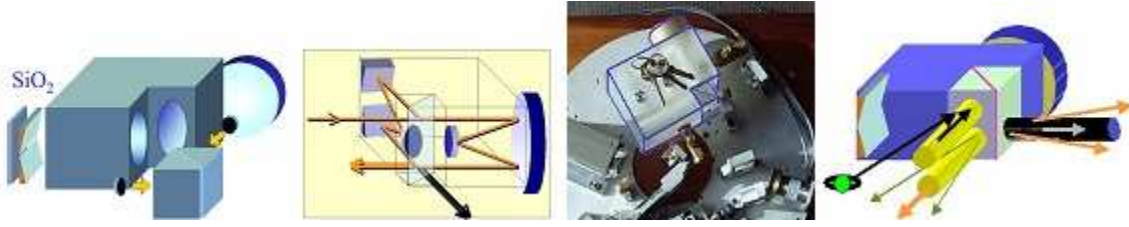


Figure 3. From left to right : the kit of elements, the life of an on-axis beam and the two exit ports, AIC itself in an optical interface for accommodation on a telescope, the making of the output beams from both on-axis and off-axis sources.

collected energy while no photon goes into the other, the destructive port. An off-axis source yields two symmetrically oriented sub-beams at each exit port. Each exiting sub-beam conveys 1/4 of the energy collected from the companion.

2.3. Formalism and algebraic description of the principle

The formalism is the one of Fourier optics (Goodman [25]), involving a pupil plane and an image plane. The cat's eye being designed in this purpose, the two arms share the same pupil plane, placed at the exit collimator, which focuses the recombined beams to the detector set in the image plane.

Coordinates are vectorial eventhough we frequently note them by a single letter. We use their reduced form (dimensionless). Thus, coordinate in pupil plane is noted ξ and means (vector in pupil plane)/(wavelength) while α is angular (radians) and means (vector in image plane)/(focal length of exit collimator). The magnification factor between entry and output pupil planes is set as unity thus α is associated to an angle over the sky, frequently noted ρ (vector). All vector coordinates are sometimes expressed using polar coordinates (ξ, ϕ) and (α, θ) or (ρ, θ) where ξ , ρ and α are then the moduli whilst ϕ and θ are the polar angles. Fig. 4 illustrates the notations used. Complex amplitudes of fields are noted $\psi_{collected}$ and ψ_{recomb} respectively at the entry and at the exit pupil planes.

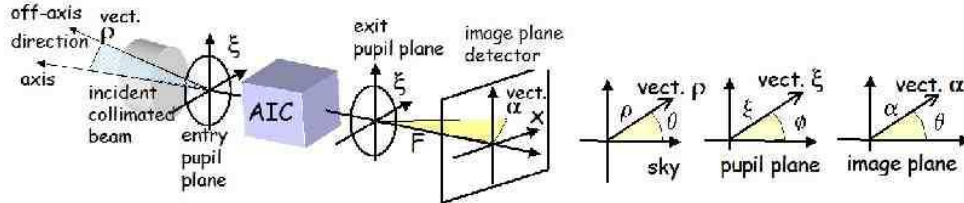


Figure 4. Schematic description of the notations used.

The transmission $P(\xi)$ at the aperture is complex. Reflection and transmission coefficients for complex amplitude at the beamsplitter are respectively noted r and t , with as usual: $R = |r|^2$ and $T = |t|^2$. Ideally $R = T = 0.5$.

2.3.1. Destructive interference process and off-axis images

The complex amplitude of the field entering AIC is $\psi_{collected}(\xi) = A.P(\xi).e^{i.\varphi(\xi)}$ since some phase distortions $\varphi(\xi)$ might exist in the collected wavefront. The field amplitude A is such that $|A|^2 = \Omega$, the brightness of the on-axis source. At recombination, each sub-field have been both transmitted and reflected at the beamsplitter. On its way each field might experience phase distortions (optical defects) and conveys the phase variation caused by propagation along the arm. In addition an extra optical path (yielding φ_{opd}) can be inserted and eventually fine-tuned in the "ff" arm. Besides, in the "fc" arm the π phase shift occurs and $\psi_{collected}(\xi)$ is symmetrized by the 180 degrees rotation of pupil, thus yielding $\psi_{collected}(-\xi)$. At recombination we have $\psi_{recomb}(\xi) = \psi_{ff}(\xi) + \psi_{fc}(\xi)$ whose explicit expression depends on the exit port. At the destructive port we have:

$$\psi_{ff}(\xi) = r.t.A.P(\xi). \left[e^{i.\varphi(\xi)} . e^{i.\varphi_{ff}(\xi)} . e^{i.\varphi_{ff-path}} . e^{i.\varphi_{opd}} \right]$$

and:

$$\psi_{fc}(\xi) = r.t.A.P(-\xi). \left[e^{i.\pi} . e^{i.\varphi(-\xi)} . e^{i.\varphi_{fc}(\xi)} . e^{i.\varphi_{fc-path}} \right].$$

At the constructive port, $\psi_{ff}(\xi)$ keeps the same expression, while the π phase shift factor $e^{i\cdot\pi}$ is replaced by unity in $\psi_{fc}(\xi)$. In these description φ_{ff} and φ_{fc} are gathering internal phase defects in respective arms. All phase terms are chromatic, but for easier reading, λ is omitted in the formulae.

In ideal situation, all mentioned phases are zero and optical paths are equal, hence we have :

$$\psi_{recomb}(\xi) = r.t.A. [P(\xi) - P(-\xi)].$$

Thus, as soon as the complex transmission is centro-symmetric ($P(\xi) = P(-\xi)$), we find that $\psi_{recomb}(\xi)$ is uniformly zero. Hence photons from the on-axis source do not reach the detector's plane (they are sent back to the sky via the constructive port). This complete cleaning of the image plane for stellar photons in ideal case is specific of AIC. Therefore, there is no geometrical link between the rejection lobe (IWA) and the energy distribution in image plane.

For a companion, off-axis by ρ , we have :

$$\psi_{collected}(\xi) = A.P(\xi).e^{-i\cdot 2\cdot\pi\cdot\xi\cdot\rho},$$

and at recombination we find :

$$\psi_{recomb}(\xi) = r.t.A.P(\xi) [e^{-i\cdot 2\cdot\pi\cdot\xi\cdot\rho} - e^{+i\cdot 2\cdot\pi\cdot\xi\cdot\rho}],$$

which is not zero, so that some light escapes the destructive process (let us note that, without the pupil rotation, we would find zero just like for the on-axis source). Besides, the system yields two twin-images of the companion, as described below, using Fourier Optics. The intensity in image plane is :

$$I(\alpha, \rho) = |\hat{\psi}_{recomb}(\alpha)|^2.$$

Since we have :

$$\hat{\psi}_{recomb}(\alpha) = r.t.\hat{P}(\alpha) * [\delta(\alpha - \rho) - \delta(\alpha + \rho)],$$

we end up (usual complex notations) with :

$$I(\alpha, \rho) = R.T.\Omega. \left[|\hat{P}(\alpha - \rho)|^2 + |\hat{P}(\alpha + \rho)|^2 - 2.Re(\hat{P}(\alpha - \rho).\hat{P}^*(\alpha + \rho)) \right],$$

that shows the presence of two twin images (centro-symmetrically located Airy patterns) and of a cross-term. This latter is vanishing as ρ is increasing (enlarged separation, product of amplitudes null). Conversely, it makes the intensity progressively cancel as ρ goes to zero (companion no longer off-axis, hence undergoing rejection). We report in Fig. 5 a pictorial summary of the destructive interference process both for star and companion, in terms of both wavefronts and complex amplitudes.

When departing from the ideal situation, all mentioned phases no longer are zero, but we still assume $P(\xi) = P(-\xi)$, the essential requirement for the coronagraph to work properly. The amplitude at recombination now is (with self-explanatory notations) :

$$\psi_{recomb}(\xi) = r.t.A.P(\xi) [e^{i\cdot\varphi_1(\xi)} - e^{i\cdot\varphi_2(\xi)}],$$

which is clearly not zero, so that a residual energy is found in image plane and rejection has a finite value, whose expression we now derive.

2.3.2. Expression of the rejection from integrated energy in image plane

In the introduction, rejection has been defined by the ratio $Rej = w_0/w$ with w and w_0 the intensities recorded respectively with and without the coronagraphic effect (in other words at destructive and constructive ports). With this definition we have in real situation :

$$Rej = \frac{w_0}{w} = \frac{\int |P(\xi).e^{i\cdot\varphi_1(\xi)} + P(-\xi).e^{i\cdot\varphi_2(\xi)}|^2 d\xi}{\int |P(\xi).e^{i\cdot\varphi_1(\xi)} - P(-\xi).e^{i\cdot\varphi_2(\xi)}|^2 d\xi}.$$

The phase factor that might occur in $P(\xi)$ is reported in the incident wavefront phase distortions, so that $P(\xi)$ is real and in addition we assume

$$P(\xi) = \Pi\left(\frac{\xi}{D}\right) = |P(\xi)|^2$$

to be the usual “camembert-like” transmission (1 inside, 0 outside the disk of diameter D). Moreover, it is reasonable to assume that the various phase terms are small, so that using the approximation $e^{i.x} = 1 + i.x + \dots$ we write :

$$Rej = \frac{\int_{pupil} (1 + \cos \Delta\varphi(\xi)) . d\xi}{\int_{pupil} (1 - \cos \Delta\varphi(\xi)) . d\xi} \approx \frac{4}{\int_{pupil} |\Delta\varphi(\xi)|^2 d\xi} = \frac{4}{\sigma_{\Delta\varphi}^2},$$

where we have introduced the differential phase $\Delta\varphi(\xi)$ such that :

$$\Delta\varphi(\xi) = [\varphi(\xi) - \varphi(-\xi)] + [\varphi_{ff}(\xi) - \varphi_{fc}(\xi)] + [\varphi_{ff-path} - \varphi_{fc-path} + \varphi_{opd}],$$

and where φ_{opd} allows adjusting to zero the mean-value, hence the use of the variance $\sigma_{\Delta\varphi}^2$. Respective expressions of integrated energy at constructive and destructive ports are $w_0 = 4.R.T.\Omega.S$ and $w = [w_0/4] . \sigma_{\Delta\varphi}^2$, where S is the area of the collecting aperture.

From the generic expression $Rej = 4/\sigma_{\Delta\varphi}^2$, the rejection can be evaluated in connection with the various phase defects and conversely, technical specifications (tolerancing) can be defined according to a targeted rejection; this is considered later in the text.

Let us note that, although this definition is a general and widespread convention, it rather traces the quality of the set-up than the ability to detect a companion, since it does not consider the shape of the energy distribution in the image plane. Therefore, for a companion imaged at a location free from residual energy, this integrated quantity is not appropriate and likely to be pessimistic. This point is also discussed later in the text.

2.3.3. Spatial response of AIC: close-sensing

To evaluate the close-sensing capability (in other words, beyond which angular separation can the companion be seen?) we consider a point-like source off-axis by ρ , and we integrate the energy in the image plane to obtain the recordable energy with respect to ρ , what describes the spatial response $w(\rho)$ of AIC ($w(\rho)$ has a circular symmetry).

With our notations the brightness distribution (using Dirac δ symbol) is $\Omega(\alpha, \rho) = \Omega.\delta(\alpha - \rho)$. Here we momentarily drop all spurious phase effects, including OPD misbalance; hence $\Delta\varphi(\xi) = 0$. We have then

$$\psi_{collected} = A.P(\xi).e^{-i.2\pi.\xi.\rho},$$

and using the Parseval-Plancherel theorem we can write :

$$w(\rho) = \int I(\alpha, \rho) . d\alpha = \int \left| \widehat{\psi}_{recomb}(\alpha, \rho) \right|^2 . d\alpha = \int |\psi_{recomb}(\xi, \rho)|^2 . d\xi.$$

More explicitly, using polar coordinates (ξ, ϕ) in pupil plane and (ρ, θ) for the off-axis direction, we write :

$$w(\rho) = 2.R.T.\Omega. \int_0^{2\pi} \int_0^{D/2} (1 - e^{-i.2\pi.(2.\xi.\rho). \cos(\phi-\theta)}) . \xi . d\xi . d\phi.$$

Thus, from Hankel’s transform properties (Bracewell [26]) we end up with the spatial transmission or rejection lobe (circular symmetry, sky coordinate ρ) :

$$w(\rho) = 2.R.T.\Omega. \left(\frac{\pi.D^2}{4} \right) . \left[1 - \frac{2.J_1(2.\pi.D.\rho)}{2.\pi.D.\rho} \right],$$

where the Airy distribution (for amplitudes) appears, associated to a telescope of diameter $2D$. Fig. 5 illustrates the radial profile of the function $w(\rho)$, showing the close-sensing capability of AIC and how it beats the diffraction-limit. Namely the maximal transmission occurs at less than the telescope’s first Airy (λ/D) ring. For an off-axis source at $\rho = 0.3$ Airy, the transmission remains 0.5 of that far from axis (Baudoz [3]).

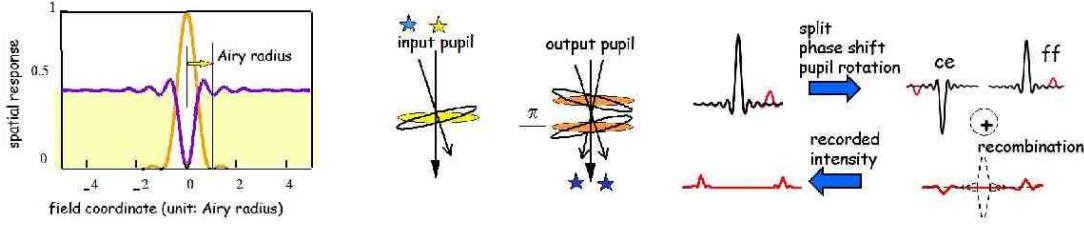


Figure 5. Left: radial profile of the spatial response of AIC (circular symmetry); Center and right: pictorial description of the destructive interference process, wavefront behaviour, amplitude behaviour.

3. Operational and technical constraints, associated limitations and theoretical capabilities

For the coronagraphic effect to work, two immediate constraints apply: (i) the complex transmission at exit pupil plane must be insensitive to a 180 degrees rotation, and the optical path difference (OPD) must accurately be zero. Other constraints concern the technical specifications and the conditions of observation.

Regarding the symmetry of the pupil, problems might arise from the amplitude of the transmission $P(\xi)$, because of the central obscuration and the spider bearing it (central-symmetry would possibly be broken). Then, by inserting a suitably designed mask in an auxiliary pupil plane, centro-symmetry is recovered; thus this constraint is not a heavy one. We report in Fig. 6 an illustration of both the trouble and the remedies. Problems regarding the phase of the complex transmission are by far more serious and are considered later in the text.

Residual Optical Path Difference (OPD) and optical defects. OPD between interfering waves works as a weight applied to the contribution of the on-axis source. As OPD goes away from zero the on-axis source gradually appears in the image, and this rapidly degrades the rejection. This is schematically illustrated in Fig. 6. Either for a residual OPD or for optical defects we use the formula $Rej = 4/\sigma_{\Delta\varphi}^2$ but in place of $\sigma_{\Delta\varphi}^2$, which makes sense only for optical defects, we directly take $[4.\pi^2/\lambda^2].\delta^2$ where δ stands for either the residual OPD or for the standard-deviation of surface defects over the pupil. Then, with a target rejection G we define the tolerance on δ via $Rej \geq G$ which yields the condition $\delta \leq \lambda/(\pi.\sqrt{G})$. For example with $G = 10^4$ the constraint on δ is roughly $\lambda/300$ and for $G = 10^5$ it is $\lambda/1000$, which are rather stringent constraints so that interferometric control is mandatory when assembling AIC. The same range of specification applies, for example, to the beamsplitting cube, where internal reflected waves must be kept destructively interfering; this is a matter of well-controlled optical paths within the cube. Moreover, phase defects occurring inside AIC cannot be corrected for, and degrade the rejection.

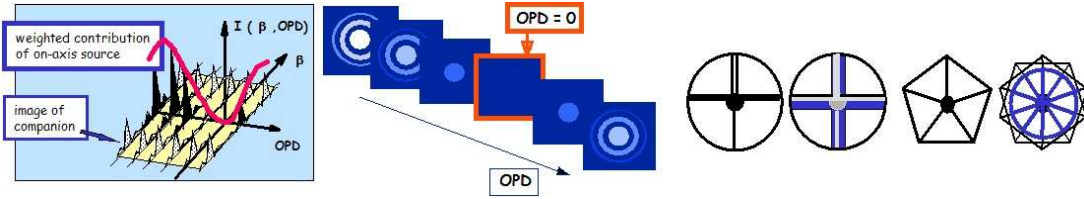


Figure 6. Left and center: pictorial illustration of the role of OPD; right: recovering amplitude centro-symmetry in the collecting aperture, by using appropriate masks in intermediate pupil plane.

3.1. Limitations from conditions of observation

Basically, stellar leakage and wavefront phase distortions are the immediate causes limiting the rejection. Stellar leakage occurs with any nulling technique, when the star has a finite angular diameter and is incompletely eliminated by the spatial response because its profile around origin is not flat. Wavefront distortions originate in deterministic optical defects (arising in the optical train) and random distortions induced by atmospheric turbulence, this latter causing the major limitation in ground-based observations (with tip/tilt fluctuations being the heaviest contributor). Another constraint occurs because of atmospheric refraction (beyond the scope of this paper). With space-based observations, beside fine guidance residual fluctuations (jitter) only faint internal phase defects are occurring and are not that big a concern (Baudoz [3]; Rabbia et al. [13]).

Stellar leakage, denoted $w(\Theta)$ for a star whose brightness distribution is $\Omega(\rho) = \Omega.\Pi(\frac{\rho}{\Theta})$ with angular diameter Θ , is evaluated by the integral of the spatial response $w(\rho)$ taken over the brightness distribution. Again from Hankel's transform properties we have :

$$w(\Theta) = \int_0^{2\pi} \int_0^{\Theta/2} w(\rho) \cdot \rho \cdot d\rho \cdot d\theta = 2.R.T.\Omega. \left[1 - \frac{J_0(\pi.D.\Theta)}{(\pi.D.\Theta)^2/4} \right].$$

As an example for $\Theta = 0.05$ Airy radius, stellar leakage (residual/collected) is 0.001 (Baudoz et al. [4]).

Random phase distortions from atmospheric turbulence. The spurious phase distribution is noted :

$$\Delta\varphi(\rho, \theta) = \varphi(\rho, \theta) - \varphi(\rho, \theta + \pi),$$

usually expressed as an infinite weighted sum of Zernike orthogonal polynomials :

$$\varphi(\rho, \theta) = \sum_{j=1}^{\infty} w_j \cdot Z_j(\rho, \theta),$$

where the w_j are random and trace the effect of turbulence. The resulting variance $\sigma_{\Delta\varphi}^2$ must be reduced by using an Adaptive Optics (AO) system. Its role is to induce appropriate phase distortions so as to absorb some of the incident ones. Note that centro-symmetric phase distortions automatically cancel, whilst other are amplified; however, a significant gain remains by using AO (Baudoz et al. [4]). For convenience, we refer to the Zernike formalism (Noll [27]) to theoretically describe the action of AO, which leads to a corrected phase distribution :

$$\varphi_{corr}(\rho, \theta) = \varphi(\rho, \theta) - \sum_{j=1}^J a_j \cdot Z_j(\rho, \theta),$$

where J is the highest Zernike order include in the correction. The resulting variance is significantly less than the previous one, and hence there is a better rejection. The result in the image is a centro-symmetric speckle pattern, whose time-averaged distribution looks like a halo (volcano+caldera-shaped). Algebraic derivation (Baudoz et al. [4]) shows that the higher J , the larger the caldera (central dark hole) and the lower the edges of the volcano. Actually, this theoretical approach pertains to ultimate performance. Practically, since AO may work in various regimes (zonal, modal, Fourier basis set) the pure Zernike formalism might depart from real situations and expected corrections are not completely efficient (what we call "incomplete correction") and estimations must be reviewed, using an example of actual AO performance (Conan [28]). Both estimates from numerical simulation are shown in Fig. 9.

Effect of residual tip/tilt phase defects. Incomplete tip/tilt correction (pointing jitter) causes the heaviest degradation and deserves a specific derivation. Taking into account that tip/tilt residuals are small, and using the approximation $2.J_1(z)/z \cong 1 - z^2/8$ the resulting average rejection is obtained from the averaged spatial response yielding :

$$< Rej > = \frac{w_0}{< w(\rho) >} \cong \frac{16}{(2\pi.D/\lambda)^2 \cdot < \rho^2 >},$$

whence is extracted the constraint :

$$\sigma_\rho \leq \frac{airy}{\sqrt{< Rej >}},$$

where $< Rej >$ is the target rejection and $airy = 1.22 \frac{\lambda}{D}$. For example, a 10^4 target leads to $\sigma_\rho \leq \frac{airy}{100}$. With HST ($D = 2.4$ m) at 2.2μ m we find $\sigma_\rho \leq 10^{-8}$ rad or 0.002 arcsec, which is in the range of the HST fine guidance capability.

3.2. theoretically expectable performance

Enhancement of detection capability by the "scaled-subtraction" process. Thanks to the large spectral bandwidth allowed by AIC, two adjacent channels splitting the K window might be accommodated on the same detector. The respective residual speckles have homothetic patterns (scaling factor : λ). Therefore, in principle (thanks to the

central “dark-hole”) it is possible to give them the same spatial distribution by properly scaling both the spatial extension and the intensity distribution. Then, images of a companion become shifted in one channel with respect to the other and have unequal heights. Subtracting the re-scaled patterns tends to eliminate the speckles while a trace of the companion remains. This process (schematically summarized in Fig. 7), is described with numerical simulations in Gay et al. [5] and Verinaud & Carillet [29]. In case of an on-axis residual spurious contribution, efficiency is reduced, but a significant gain in detection capability remains.

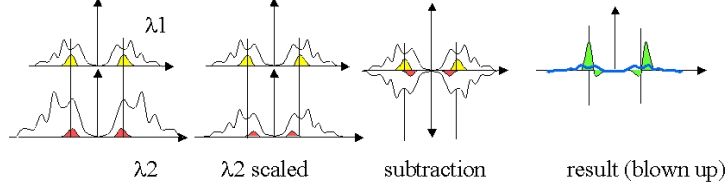


Figure 7. Pictorial summary of the scaled-subtraction process.

Signal to Noise ratio for the detection of a companion. As already mentioned, using the integrated rejection $Rej = 4/\sigma_{\Delta\varphi}^2$ is not appropriate to evaluate the detection capability for a companion, the point being not to count unwanted photons in the whole image plane, but rather to distinguish the companion against the noisy and non-uniform residual energy distribution. Thus the convenient approach for theoretical assessments is to express a pixel-dependent Signal to Noise Ratio (SNR), taking into account the spatial response of AIC, the intensity fluctuations (speckled halo) and the area covered by the companion’s image (distance to axis and image extension). From a detailed analysis (Baudoz et al. [4]) the expression of this SNR, (M recorded exposures, companion off-axis by angular vector ρ) is :

$$SNR(\rho) = \frac{(N_c/4) \cdot \sqrt{2} \cdot \sqrt{M} \cdot \int_{companion} w(\alpha) \cdot C(\alpha - \rho) \cdot d\alpha}{\sqrt{\int_{companion} [var_{residual}(\alpha) + var_{bg} + var_{detect}] \cdot d\alpha}},$$

where the factor $1/4$ traces the transmission for a single image, $\sqrt{2}$ accounts for the two twin-images, $w(\rho)$ is the spatial response of AIC, and $C(\alpha - \rho)$ is the normalized distribution weighting of the companion’s contribution (Airy-like shaped). Integration is taken over the pixels covered by the companion’s image.

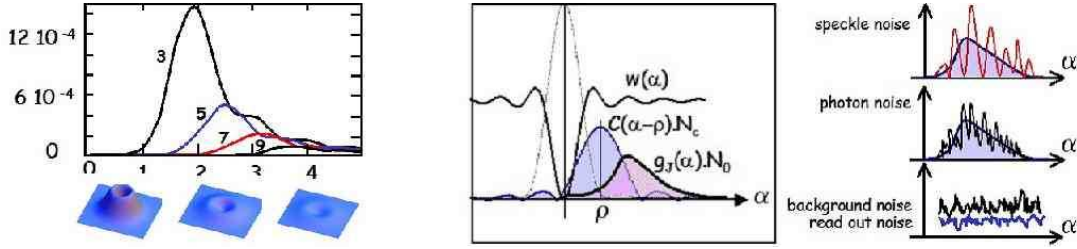


Figure 8. Left : residual energy profiles with AO corrections up to 9 Zernike radial orders (meaning $J = 36$); center : notations for the SNR expression (only one-sided cuts featured); right : phenomenology of noises in the residual energy.

The number of collected photons from a m -magnitude star is :

$$N_0 = [F_{ref}(\lambda)/h\nu] \cdot 10^{-0.4 m} \cdot [\eta \cdot A \cdot R \cdot T \cdot S \cdot t_{opt} \cdot \Delta\lambda \cdot \tau],$$

with usual notations, while for the companion (magnitude difference Δm) we have :

$$N_c = N_0 \cdot 10^{-0.4 \Delta m}.$$

In the noise factor, variances are related to a given pixel : var_{det} is the readout noise variance (ron^2) of the detector, var_{bg} is for the background radiation (using Planck’s formulae) and $var_{residual}$ comes from the fluctuations of the residual energy distribution. This latter includes $g_J \cdot N_0$ the residual energy when AO-corrections are carried up to the Zernike radial order J (each comprising several azimuthal orders), and is evaluated by the doubly stochastic process involving the Poisson photon noise at a given illumination level and the fluctuations of this level. Performance of AIC (expressed as detectable Δm , directly depends on AO capabilities (Fig. 8).

Illustrations for “complete” and “incomplete” corrections are given in Fig. 9 as well as expectable detection capabilities in space-based observation.

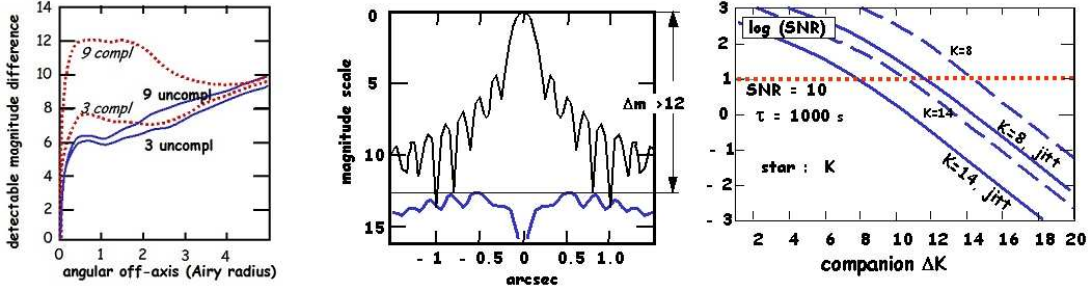


Figure 9. Left : theoretically detectable magnitude difference of a companion versus its off-axis angle, showing both complete (ideal) and incomplete (real) AO corrections, for radial orders 3 and 9, calculated for expectable conditions at CFHT, Hawaii : $r_0 = 30$ cm, $\tau = 0.1''$, SNR= 5 for target $K = 5$; (see Baudoz et al.[4,12]). Center : numerical simulation (based on a phase error map of HST) of residual energy profile for observation in K window ($2.2\mu\text{m}$; $\Delta\lambda = 0.4\mu\text{m}$), and expressed in magnitude differences. Right : behaviour of SNR versus ΔK the magnitude difference between star and companion; curves pertain to star K magnitudes 8 and 14. Dashed lines : optical quality is assumed the same as on HST, pointing instabilities eliminated. Solid lines : pointing residuals of 5 mas rms causes less than 3 magnitudes degradation. K window, quantum efficiency $\eta = 0.5$, $R = T = 0.5$, $S = 50\text{m}^2$, optical transmission $t_{opt} = 0.1$, observing time 1000 sec, ron= 20e/pix.

4. Results

The results obtained so far both in laboratory and “on the sky” are but illustrations of potential capabilities. To spare space we rely on a pictorial presentation, see Fig. 10 and Baudoz et al. [4,12] for details.

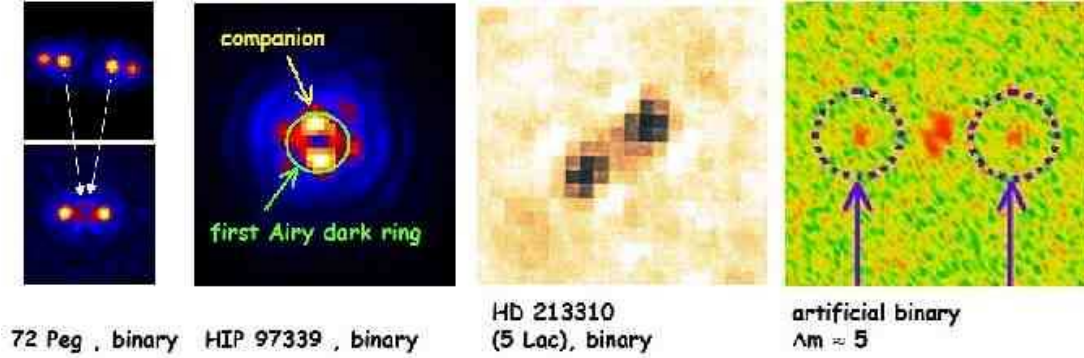


Figure 10. Left, center left, center right : celestial sources, $\lambda = 2.2\mu\text{m}$,

Close-sensing capability is clearly validated. Effective capability for the detection is in good agreement between expected and observed capabilities, taking into account the turbulence conditions and the AO performance.

5. Conclusion

In this article we have presented the main and specific features of our Achromatic Interfero Coronagraph (principle, theoretical capabilities and some results from test runs in laboratory and behind a telescope). The main advantages of AIC are the large spectral bandwidth over which the coronagraphic rejection is achievable and the very small Inner Working Angle (providing the capability to explore the very close angular neighbouring of a source at a level better than set by the diffraction limit). The main drawback is the difficulty to achieve and to maintain equality of the optical paths at the required accuracy. Recently, an improved version of the

device (regarding OPD fine-tuning) has been built and is presently under test. The future step is to accommodate this new AIC on a large telescope equipped with Adaptive Optics, so as to undertake scientific programs. New configurations, easier to accommodate in a telescope's optical train are currently under study.

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